# Product operator descriptions of INEPT and RINEPT NMR spectroscopies for $I S_{n}(I=1 / 2, S=3 / 2)$ spin systems 

Ahmet Tokatl1, ${ }^{\text {a }}$ Azmi Gençten, ${ }^{\text {b }}$ Mükerrem Şahin, ${ }^{\text {a }}$ Özden Tezel, ${ }^{\text {b, }}{ }^{1}$ and Semiha Bahçeli ${ }^{\text {a,* }}$<br>${ }^{a}$ Department of Physics, Faculty of Arts and Sciences, Süleyman Demirel University, Isparta, Turkey<br>${ }^{\text {b }}$ Department of Physics, Faculty of Arts and Sciences, Ondokuz Mayis University, Samsun, Turkey

Received 4 August 2003; revised 26 February 2004
Available online 10 May 2004


#### Abstract

The product operator descriptions of INEPT and reverse INEPT (RINEPT) NMR experiments are introduced for weakly coupled $I S_{n}(I=1 / 2, S=3 / 2$ with $n=1,2,3)$ spin systems. Explicit expressions for polarization transfer from spin-3/2 quadrupolar nuclei to spin- $1 / 2$ nuclei (and reversed polarization transfer) are given in detail by using the evolutions of product operators under the spin-spin coupling Hamiltonian. The results calculated for the intensities and positions of the observable signals are simulated in the molecules containning the ${ }^{119} \mathrm{Sn}(I=1 / 2)$ and ${ }^{35} \mathrm{Cl}(S=3 / 2)$ nuclei at the coupling constant of $J_{\mathrm{Sn}-\mathrm{Cl}}=375 \mathrm{~Hz}$ by using the Maple programme on computer.


© 2004 Elsevier Inc. All rights reserved.

Keywords: NMR spectroscopy; Spin-spin coupling Hamiltonian; Polarization transfer; INEPT and RINEPT pulse sequences; Product operator formalism

## 1. Introduction

The NMR signals of insensitive nuclear spins can be enhanced by transferring polarization from a more sensitive species to which they are coupled [1]. The wellknown pulse sequences as the polarization transfer techniques are insensitive nuclei enhanced by polarization transfer (INEPT), distortionless enhancement by polarization transfer (DEPT), and reverse insensitive nuclei enhanced by polarization transfer (RINEPT) $[2,3]$. The INEPT sequence is an alternative to the nuclear Overhauser effect. The INEPT experiment does not require any particular relaxation mechanism and therefore a better enhancement factor can be obtained [1]. Furthermore it is demonstrated that INEPT sequence can be used to determine the multiplicity of each signal in a ${ }^{13} \mathrm{C}$ NMR spectrum [3]. More recently, the INEPT and DEPT experiments were used for the coherence

[^0]transfer via heteronuclear $J$-coupling between spin-1/2 and quadrupolar nuclei in the solids [4-6]. Fyfe et al. [4] showed that coherence transfer via the scalar coupling between spin-1/2 and quadrupolar nuclei can be obtained in the solid state by using INEPT experiment.

On the other hand to analyse and describe the multipulse NMR experiments an effective and useful tool is product operator theory as a simple quantum mechanical method [7,8]. The product operator formalism has been used for weakly coupled $I S(I=1 / 2 ; S=1 / 2,1$, and $3 / 2$ ) spin systems [7,9-12]. The polarization transfer (PT) between spin- $1 / 2$ nuclei in an INEPT pulse sequence has been described by using product operator theory [13]. Chandrakumar [14] investigated the polarization transfer between spin-1 and spin-1/2 nuclei by using product operator formalism for INEPT and from spin-1/ 2 to spin-1 nuclei for refocusing INEPT experiments.

In our present work we first introduce the results of the applications of the product operators theory to the polarization transfer between spin- $3 / 2$ and spin- $1 / 2$ nuclei for INEPT and from spin-1/2 to spin-3/2 nuclei for RINEPT experiments. As one practical application of this theory we have taken the molecules that include one
of these three organometallic compounds: trimethyltinchloride $\left[(\mathrm{CH})_{3} \mathrm{SnCl}\right]$ (as $I S$ spin system), dimethyltindichloride $\left[\left(\mathrm{CH}_{3}\right)_{2} \mathrm{SnCl}_{2}\right]$ (as $I S_{2}$ spin system) and methyltintrichloride $\left[\mathrm{CH}_{3} \mathrm{SnCl}_{3}\right]$ (as $I S_{3}$ spin system) containing the weakly coupled $I=1 / 2\left({ }^{19} \mathrm{Sn}\right.$ with $\gamma=$ $\left.-9.53 \times 10^{7} \mathrm{~T}^{-1} \mathrm{~s}^{-1} ; 8.58 \%\right)$ and $S=3 / 2\left({ }^{35} \mathrm{Cl}\right.$ with $\gamma=$ $2.62 \times 10^{7} \mathrm{~T}^{-1} \mathrm{~s}^{-1} ; 75.53 \%$ ) nuclei $[15,16]$. It is well know that the scalar or indirect coupling $J$ to the quadrupolar nuclei can be observed provided that some arrangements of ligands can cause to give low or zero electric field gradients at a point of the molecule [17,18]. In this framework by considering the values mentioned above in our selected real chemical systems the coupling constant $J_{\mathrm{Sn}-\mathrm{Cl}}$ was taken as 375 Hz and simulate the intensities and positions of observable signals in INEPT and RINEPT by using Maple programme on computer [19,20].

### 1.1. Polarization transfer between spin-3/2 and spin-1/2 nuclei in INEPT and reverse INEPT experiments

To describe the INEPT and reverse INEPT (RINEPT) NMR experiments by using product operator formalism for weakly coupled $I S(I=1 / 2, S=3 / 2)$ spin systems we consider that the spin multiplicity of $I$ can be decomposed into in-phase and anti-phase coherence with the inner and outer transitions of multiplet [7,11]. For the evolutions of product operators under spin-spin coupling Hamiltonian it is convenient to use the wellknown Hausdorff formula [21].

Then, the evolutions of $I_{x}, I_{y}, I_{x} S_{z}$, and $I_{y} S_{z}$ product operators under the spin-spin coupling Hamiltonian can be written as [11]:

$$
\begin{aligned}
I_{x} \xrightarrow{2 \pi J_{z} S_{z} t} & I_{x} E_{s}\left( \pm \frac{3}{2}\right) \cos (3 \pi J t)+\frac{2}{3} I_{y} S_{z} E_{s}\left( \pm \frac{3}{2}\right) \sin (3 \pi J t) \\
& +I_{x} E_{s}\left( \pm \frac{1}{2}\right) \cos (\pi J t)+2 I_{y} S_{z} E_{s}\left( \pm \frac{1}{2}\right) \sin (\pi J t) \\
I_{y} \xrightarrow{2 \pi J I_{z} S_{z} t} & I_{y} E_{s}\left( \pm \frac{3}{2}\right) \cos (3 \pi J t)-\frac{2}{3} I_{x} S_{z} E_{s}\left( \pm \frac{3}{2}\right) \sin (3 \pi J t) \\
& +I_{y} E_{s}\left( \pm \frac{1}{2}\right) \cos (\pi J t)-2 I_{x} S_{z} E_{s}\left( \pm \frac{1}{2}\right) \sin (\pi J t)
\end{aligned}
$$

$$
\begin{align*}
I_{x} S_{z} \xrightarrow{2 \pi J I_{z} S_{z} t} & I_{x} S_{z} E_{s}\left( \pm \frac{3}{2}\right) \cos (3 \pi J t)+\frac{3}{2} I_{y} E_{s}\left( \pm \frac{3}{2}\right) \sin (3 \pi J t)  \tag{1c}\\
& +I_{x} S_{z} E_{s}\left( \pm \frac{1}{2}\right) \cos (\pi J t)+\frac{1}{2} I_{y} E_{s}\left( \pm \frac{1}{2}\right) \sin (\pi J t)
\end{align*}
$$

and

$$
\begin{align*}
I_{y} S_{z} \xrightarrow{2 \pi J I_{z} S_{z} t} & I_{y} S_{z} E_{s}\left( \pm \frac{3}{2}\right) \cos (3 \pi J t)-\frac{3}{2} I_{x} E_{s}\left( \pm \frac{3}{2}\right) \sin (3 \pi J t) \\
& +I_{y} S_{z} E_{s}\left( \pm \frac{1}{2}\right) \cos (\pi J t)-\frac{1}{2} I_{x} E_{s}\left( \pm \frac{1}{2}\right) \sin (\pi J t) \tag{1d}
\end{align*}
$$

We used these expressions for the descriptions of INEPT and RINEPT pulse sequences. Figs. 1a and b show the mentioned pulse sequences, respectively. The labelled numbers on Fig. 1 indicate the density matrix operators at each stage of the experiments.

For the $I S$ spin system the density matrix operators calculated at the first five stages of INEPT pulse sequence are listed in Table 1.

As seen in Table 1 and in Fig. 1b, the effects of spinspin coupling Hamiltonian, $H_{J}=2 \pi J I_{z} S_{z}$, on the product operators are considered at the intervals 1-2 and 3-4 stages for mentioned pulse sequence. Since the time interval between applied pulses $\tau=1 / 4 J$, we take $C_{2 J}=0$ and $S_{2 J}=1$ for $\sigma_{4}$ density matrix operator. In the last stage of INEPT experiment, by considering first the chemical shift and then spin-spin coupling effects we get

$$
\begin{align*}
& \sigma_{6}=-2 b I_{y} S_{z} E_{s}\left( \pm \frac{3}{2}\right) C_{I} C_{3 J}+3 b I_{x} E_{s}\left( \pm \frac{3}{2}\right) C_{I} S_{3 J} \\
& +2 b I_{x} S_{z} E_{s}\left( \pm \frac{3}{2}\right) S_{I} C_{3 J}+3 b I_{y} E_{s}\left( \pm \frac{3}{2}\right) S_{I} S_{3 J} \\
& -2 b I_{y} S_{z} E_{s}\left( \pm \frac{1}{2}\right) C_{I} C_{J}+b I_{x} E_{s}\left( \pm \frac{1}{2}\right) C_{I} S_{J} \\
& +2 b I_{x} S_{z} E_{S}\left( \pm \frac{1}{2}\right) S_{I} C_{J}+b I_{y} E_{s}\left( \pm \frac{1}{2}\right) S_{I} S_{J} \\
& -a I_{x} E_{s}\left( \pm \frac{3}{2}\right) S_{I} C_{3 J}-a I_{x} E_{s}\left( \pm \frac{1}{2}\right) S_{I} C_{J}, \tag{2}
\end{align*}
$$

Fig. 1. (a) Conventional INEPT pulse sequence for the polarization from $S=3 / 2$ nuclei to $I=1 / 2$ nuclei and (b) reversed INEPT (RINEPT) pulse sequence for the polarization from $I=1 / 2$ nuclei to $S=3 / 2$ nuclei $(\tau=1 / 4 J)$.

Table 1
For $I S(I=1 / 2, S=3 / 2)$ spin systems, the calculated first five density matrix operators in INEPT pulse sequence

$$
\begin{aligned}
& \text { INEPT } \\
& \sigma_{0}=b S_{z}+a I_{z} \\
& \sigma_{1}=-b S_{y}+a I_{z} \\
& \sigma_{2}=-b\left(S_{y} C_{J}^{\prime}-2 I_{z} S_{x} S_{J}^{\prime}\right)+a I_{z} \\
& \sigma_{3}=-\sigma_{2} \\
& \mathrm{Using} \cos (2 \pi J \tau)=0, \sin (2 \pi J \tau)=1 \text { since } \tau=1 / 4 J \\
& \sigma_{4}=-2 b I_{z} S_{x}-a I_{z} \\
& \sigma_{5}=-2 b I_{y} S_{z} E_{s}\left( \pm \frac{3}{2}\right)-2 b I_{y} S_{z} E_{s}\left( \pm \frac{1}{2}\right)+a\left[I_{y} E_{s}\left( \pm \frac{3}{2}\right)+I_{y} E_{s}\left( \pm \frac{1}{2}\right)\right] \\
& \hline
\end{aligned}
$$

Where $C_{n J}^{\prime}=\cos (n \pi J \tau)$ and $S_{n J}^{\prime}=\sin (n \pi J \tau)$.
where $C_{n J}=\cos (n \pi J t), S_{n J}=\sin (n \pi J t), C_{I}=\cos \left(\Omega_{I} t\right)$, and $S_{I}=\sin \left(\Omega_{I} t\right)$. On the other hand since we take only single quantum terms and detect along $y$-axis, we have

$$
\begin{align*}
\sigma_{6}= & 3 b I_{y} E_{s}\left( \pm \frac{3}{2}\right) S_{I} S_{3 J}+b I_{y} E_{s}\left( \pm \frac{1}{2}\right) S_{I} S_{J} \\
& +a I_{y} E_{s}\left( \pm \frac{3}{2}\right) C_{I} C_{3 J}+a I_{y} E_{s}\left( \pm \frac{1}{2}\right) C_{I} C_{J} \tag{3}
\end{align*}
$$

If a second experiment is performed with a $90_{-y}^{0}$ pulse instead $90_{y}^{0}$ pulse on $S$ spin, then we can write

$$
\begin{align*}
\sigma_{6}= & -b\left[3 I_{y} E_{S}\left( \pm \frac{3}{2}\right) S_{3 J} S_{I}+I_{y} E_{S}\left( \pm \frac{1}{2}\right) S_{J} S_{I}\right] \\
& +a\left[I_{y} E_{s}\left( \pm \frac{3}{2}\right) C_{3 J} C_{I}+I_{y} E_{s}\left( \pm \frac{1}{2}\right) C_{J} C_{I}\right] \tag{4}
\end{align*}
$$

When the second $\sigma_{6}$ is subtracted from the first the final result becomes
$\sigma_{f}=6 b I_{y} E_{s}\left( \pm \frac{3}{2}\right) S_{3 J} S_{I}+2 b I_{y} E_{s}\left( \pm \frac{1}{2}\right) S_{J} S_{I}$.
Thus the observable magnetization for INEPT experiment is
$M_{x}(t) \alpha\left\langle I_{y}\right\rangle=\operatorname{Tr}\left[I_{y} \sigma_{f}\right]$,
and for the $I S(I=1 / 2$ and $S=3 / 2)$ spin system by substituting Eq. (5) into Eq. (6) we have the coefficients

$$
\begin{equation*}
\operatorname{Tr}\left[I_{y} I_{y} E_{s}\left( \pm \frac{3}{2}\right)\right]=\operatorname{Tr}\left[I_{y} I_{y} E_{s}\left( \pm \frac{1}{2}\right)\right]=1 \tag{7}
\end{equation*}
$$

and we obtain

$$
\begin{align*}
\left\langle I_{y}\right\rangle(I S)= & 3 b\left[\cos \left(\Omega_{I}-3 \pi J\right) t-\cos \left(\Omega_{I}+3 \pi J\right) t\right] \\
& +b\left[\cos \left(\Omega_{I}-\pi J\right) t-\cos \left(\Omega_{I}+\pi J\right) t\right] \tag{8}
\end{align*}
$$

This equation represents four signals at the coordinates of $\left(\frac{3 J}{2}, \Omega_{I}\right),\left(\frac{J}{2}, \Omega_{I}\right),\left(-\frac{J}{2}, \Omega_{I}\right)$, and $\left(-\frac{3 J}{2}, \Omega_{I}\right)$ with an intensity distribution of $(-3:-1: 1: 3)$.

For the $I S_{2}(I=1 / 2, S=3 / 2)$ spin systems in INEPT pulse sequences we can divide $I_{y}$ into four parts as

$$
\begin{align*}
I_{y}= & I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{3}{2}\right)+I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{1}{2}\right) \\
& +I_{y} E_{s}\left( \pm \frac{1}{2}, \pm \frac{1}{2}\right)+I_{y} E_{s}\left( \pm \frac{1}{2}, \pm \frac{3}{2}\right) \tag{9}
\end{align*}
$$

where, for example,
$I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{1}{2}\right)=I_{y} \otimes E_{s 1}\left( \pm \frac{3}{2}\right) \otimes E_{s 2}\left( \pm \frac{1}{2}\right)$.
By using the same considerations at every single stage of INEPT experiment seen in Fig. 1A we obtain the observable signal as

$$
\begin{align*}
\left\langle I_{y}\right\rangle\left(I S_{2}\right)=b\{ & 6\left[\cos \left(\Omega_{I}-6 \pi J\right) t-\cos \left(\Omega_{I}+6 \pi J\right) t\right] \\
& +8\left[\cos \left(\Omega_{I}-4 \pi J\right) t-\cos \left(\Omega_{I}+4 \pi J\right) t\right] \\
& \left.+6\left[\cos \left(\Omega_{I}-2 \pi J\right) t-\cos \left(\Omega_{I}+2 \pi J\right) t\right]\right\} \tag{11}
\end{align*}
$$

Thus we have seven signals at the coordinates of $\left(3 J, \Omega_{I}\right),\left(2 J, \Omega_{I}\right),\left(J, \Omega_{I}\right),\left(0, \Omega_{I}\right),\left(-J, \Omega_{I}\right),\left(-2 J, \Omega_{I}\right)$, and $\left(-3 J, \Omega_{I}\right)$ with an intensity of (-3:-4:-3:0:3:4:3).

For the $I S_{3}$ spin system in INEPT experiment we can divide $I_{y}$ into eight parts as

$$
\begin{align*}
I_{y}= & I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{3}{2}, \pm \frac{3}{2}\right)+I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{3}{2}, \pm \frac{1}{2}\right) \\
& +I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{1}{2}, \pm \frac{3}{2}\right)+I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{1}{2}, \pm \frac{1}{2}\right) \\
& +I_{y} E_{s}\left( \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{3}{2}\right)+I_{y} E_{s}\left( \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{1}{2}\right) \\
& +I_{y} E_{s}\left( \pm \frac{1}{2}, \pm \frac{1}{2}, \pm \frac{3}{2}\right)+I_{y} E_{s}\left( \pm \frac{1}{2}, \pm \frac{1}{2}, \pm \frac{1}{2}\right) \tag{12}
\end{align*}
$$

where, for instance,

$$
\begin{align*}
& I_{y} E_{s}\left( \pm \frac{3}{2}, \pm \frac{3}{2}, \pm \frac{1}{2}\right) \\
& \quad=I_{y} \otimes E_{s 1}\left( \pm \frac{3}{2}\right) \otimes E_{s 2}\left( \pm \frac{3}{2}\right) \otimes E_{s 3}\left( \pm \frac{1}{2}\right) \tag{13}
\end{align*}
$$

By following the same calculations steps we get:

$$
\begin{align*}
\left\langle I_{y}\right\rangle\left(I S_{3}\right)= & 9 b\left[\cos \left(\Omega_{I}-9 \pi J\right) t-\cos \left(\Omega_{I}+9 \pi J\right) t\right] \\
& +21 b\left[\cos \left(\Omega_{I}-7 \pi J\right) t-\cos \left(\Omega_{I}+7 \pi J\right) t\right] \\
& +30 b\left[\cos \left(\Omega_{I}-5 \pi J\right) t-\cos \left(\Omega_{I}+5 \pi J\right) t\right] \\
& +30 b\left[\cos \left(\Omega_{I}-3 \pi J\right) t-\cos \left(\Omega_{I}+3 \pi J\right) t\right] \\
& +12 b\left[\cos \left(\Omega_{I}-\pi J\right) t-\cos \left(\Omega_{I}+\pi J\right) t\right] \tag{14}
\end{align*}
$$

This equation denotes 10 signals at the coordinates of $\left(\frac{9}{2} J, \Omega_{I}\right),\left(\frac{7}{2} J, \Omega_{I}\right),\left(\frac{5}{2} J, \Omega_{I}\right),\left(\frac{3}{2} J, \Omega_{I}\right),\left(\frac{1}{2} J, \Omega_{I}\right),\left(-\frac{1}{2} J\right.$, $\left.\Omega_{I}\right),\left(-\frac{3}{2} J, \Omega_{I}\right),\left(-\frac{5}{2} J, \Omega_{I}\right),\left(-\frac{7}{2} J, \Omega_{I}\right)$, and $\left(-\frac{9}{2} J, \Omega_{I}\right)$ with an intensity distribution ( $-3:-7:-10:-10:-4: 4$ : 10:10:7:3). Figs. 2A-C show the plots of signals obtained for $I S, I S_{2}$, and $I S_{3}$ spin systems, respectively in which were performed in Maple by considering the typical coupling constant value of $J_{\mathrm{Sn}-\mathrm{Cl}}=375 \mathrm{~Hz}$ and the transverse relaxation time value of 0.01 s and the chemical shift value $\delta_{(\mathrm{Sn})}=0 \mathrm{ppm}$ for the selected molecules containing ${ }^{119} \mathrm{Sn}\left\{{ }^{35} \mathrm{Cl}\right\}$ nuclei $[19,20]$.

As for reverse INEPT (or RINEPT) experiment in which polarization transfer (PT) is from spin- $1 / 2$ nuclei to spin- $3 / 2$ nuclei, we follow the similar ways and considerations in order to get the signals for $I S(I=1 / 2$, $S=3 / 2$ ) spin system. In this framework, both the chemical shift Hamiltonian $H_{\mathrm{CS}}=\Omega_{S} S_{z}$ and spin-spin coupling Hamiltonian $H_{J}=2 \pi J I_{z} S_{z}$ are applied on the spin density operator $\sigma_{5}$ in Table 2 during acquisition time $t$ and by considering single quantum terms and the phase cycling for reverse INEPT pulse sequences we obtain


Fig. 2. Simulated spectra of weakly coupled ${ }^{119} \mathrm{Sn}\left\{{ }^{81} \mathrm{Cl}\right\}$ INEPT NMR of the selected molecules (A) for the $I S(I=1 / 2, S=3 / 2)$ spin system, (B) for the $I S_{2}$ spin system, and (C) for the $I S_{3}$ spin system.

Table 2
For $I S(I=1 / 2, S=3 / 2)$ spin systems, the calculated first five density matrix operators in reverse INEPT (RINEPT) pulse sequence

$$
\begin{aligned}
& \text { REVERSE INEPT } \\
& \hline \sigma_{0}=a I_{z}+b S_{z} \\
& \sigma_{1}=-a I_{y}+b S_{z} \\
& \sigma_{2}=-a I_{y} E_{s}\left( \pm \frac{3}{2}\right) C_{3, J}^{\prime}+\frac{2}{3} a I_{x} S_{z} E_{s}\left( \pm \frac{3}{2}\right) S_{3 J}^{\prime} \\
& \\
& \quad-a I_{y} E_{s}\left( \pm \frac{1}{2}\right) C_{J}^{\prime}+2 a I_{x} S_{z} E_{s}\left( \pm \frac{1}{2}\right) S_{J}^{\prime}+b S_{z} \\
& \sigma_{3}= \\
& \text { Using } \cos (2 \pi J \tau)=0, \sin (2 \pi J \tau)=1 \text { since } \tau=1 / 4 J \\
& \sigma_{4}= \\
& \sigma_{5}=\frac{2}{3} a I_{x} I_{z} I_{z}\left( \pm \frac{3}{2} S_{y} E_{s}\left( \pm \frac{3}{2}\right)-2 a I_{x} S_{z} E_{s}\left( \pm \frac{1}{2}\right)-b S_{z}\right. \\
& \hline
\end{aligned}
$$

Where $C_{n J}^{\prime}=\cos (n \pi J \tau)$ and $S_{n J}^{\prime}=\sin (n \pi J \tau)$.


Fig. 3. Simulated spectrum of weakly coupled ${ }^{119} \mathrm{Sn}\left\{{ }^{35} \mathrm{Cl}\right\}$ RINEPT NMR of the selected molecule (as the $I S(I=1 / 2, S=3 / 2)$ spin system).
$\sigma_{f}=-\frac{2}{3} a S_{y} E_{s}\left( \pm \frac{3}{2}\right) S_{S} S_{J}+2 a S_{y} E_{s}\left( \pm \frac{1}{2}\right) S_{S} S_{J}$.
Since the observable magnetization is defined as
$M_{y}(t) \alpha\left\langle S_{y}\right\rangle=\operatorname{Tr}\left[S_{y} \sigma_{f}\right]$
and using the coefficients
$\operatorname{Tr}\left[S_{y} S_{y} E_{s}\left( \pm \frac{3}{2}\right)\right]=\frac{3}{2}$
and
$\operatorname{Tr}\left[S_{y} S_{y} E_{s}\left( \pm \frac{1}{2}\right)\right]=\frac{7}{2}$,
finally we get

$$
\begin{align*}
\left\langle S_{y}\right\rangle(I S) & =6 a S_{S} S_{J} \\
& =3 a\left[\cos \left(\Omega_{s}-\pi J\right) t-\cos \left(\Omega_{s}+\pi J\right) t\right] . \tag{17}
\end{align*}
$$

Therefore, for RINEPT pulse sequences we have only two signals at the coordinates of $\left(\frac{J}{2}, \Omega_{S}\right)$ and $\left(-\frac{J}{2}, \Omega_{S}\right)$ with an intensity distribution of $(-1: 1)$. The simulations of these two signals for the selected molecule, trimethyltinchloride $\left[(\mathrm{CH})_{3} \mathrm{SnCl}\right]$ (as $I S$ spin system), are shown in Fig. 3.

For RINEPT experiment we have only two signals for $I S_{2}$ and $I S_{3}(I=1 / 2, S=3 / 2)$ spin systems as we detect always on the spin- $3 / 2$ nuclei along $y$-axis. The simulations of these two signals are shown in Fig. 3.

## 2. Results and discussion

It is well known that the INEPT NMR experiment is one of the most popular heteronuclear multi-pulse experiments and was initially designed to enhance the sensitivity of observing low- $\gamma$ nuclei by means of polarization transfer. In this study first we have presented the descriptions of INEPT NMR experiment for $I S_{n}$ ( $I=1 / 2, S=3 / 2$ with $n=1,2,3$ ) and reverse INEPT
(or RINEPT) NMR experiment for $I S \quad(I=1 / 2$, $S=3 / 2$ ) weakly coupled spin systems by using the product operator formalism. Approximately two-thirds of the NMR active nuclei in the periodic table are quadrupolar and therefore the NMR studies of quadrupolar nuclei are crucial. However, $J$ coupling to these fast relaxing nuclei can not be often observable. But when the quadrupolar nuclei have zero electric field gradient in some symmetries of molecules, multiplet structure can be arised from spin-spin coupling and observed [17]. In INEPT NMR experiment the final spectrum should contain responses from those spin-3/2 nuclei which are coupled to spin- $1 / 2$ nuclei. This case can be satisfy by using phase cycling schemes of the mentioned pulse sequences. In this framework Rinaldi and Baldwin [22] showed that the polarization transfer from low gamma quadrupolar nuclei $\left({ }^{1} \mathrm{H}\left\{{ }^{11} \mathrm{~B}\right\}\right)$ to $I=1 / 2$ nucleus in the $\left({ }^{1} \mathrm{H}\left\{{ }^{11} \mathrm{~B}\right\}\right)$ INEPT experiment can produce the maximum enhancement in theoretical base.

Since the INEPT experiment is usually recommended for nuclei having negative $\gamma$ values, ${ }^{29} \mathrm{Si},{ }^{119} \mathrm{Sn}$, and ${ }^{15} \mathrm{~N}$ being three examples and should be used only if one $J$ value is involved and its magnitude is know, in three organotin complexes we have taken as the real chemical systems, namely, trimethyltinchloride $\left[(\mathrm{CH})_{3} \mathrm{SnCl}\right]$ (as $I S$ spin system), dimethyltindichloride $\left[(\mathrm{CH})_{2} \mathrm{SnCl}_{2}\right]$ (as $I S_{2}$ spin system) and methyltintrichloride $\left[\mathrm{CH}_{3} \mathrm{SnCl}_{3}\right]$ (as $I S_{3}$ spin system) these conditions could be satisfied.

In our work for weakly coupled $I S(I=1 / 2, S=3 / 2)$ spin system in INEPT experiment in which PT is from spin- $3 / 2$ to spin- $1 / 2$ nuclei by using phase cycling we obtained four signals with an intensity distribution of ( $-3:-1: 1: 3$ ). This result is in very good agreement with some experimental results [22]. Furthermore the simulations of the signal intensities calculated of a selected molecules containing ${ }^{119} \mathrm{Sn}\left\{{ }^{35} \mathrm{Cl}\right\}$ nuclei by using INEPT and RINEPT pulse sequences were performed in the Maple programme on computer and the spectra obtained justify the above discussions.

## References

[1] R. Freeman, A Handbook of Nuclear Magnetic Resonance, Longman Scientific and Technical, New York, 1988, pp.157-162.
[2] G.A. Morris, R. Freeman, Enhancement of nuclear magnetic resonan signals by polarization transfer, J. Am. Chem. Soc. 101 (1979) 760-762.
[3] D.M. Doddrell, D.T. Pegg, M.R. Bendall, Distortionless enhancement of NMR signals by polarization transfer, J. Magn. Reson. 48 (1982) 323-327.
[4] C.A. Fyfe, K.C. Wong-Moon, Y. Huang, H. Grondey, INEPT experiments in solid-state NMR, J. Am. Chem. Soc. 117 (1995) 10397-10398.
[5] H.M. Kao, C.P. Grey, INEPT Experiments involving quadrupolar nuclei in solids, J. Magn. Reson. 133 (1998) 313-323.
[6] T.T. Nakashima, R.E.D. McClung, B.K. Jhon, Experimental and theoretical investigation of ${ }^{2} \mathrm{D}-{ }^{13} \mathrm{C}$ DEPT spectra on $\mathrm{CD}_{n}$ systems, J. Magn. Reson. 58 (1984) 27-36.
[7] O.W. Sorensen, G.W. Eich, M.H. Levitt, G. Bodenhausen, R.R. Ernst, Product operator formalism for the description of NMR pulse experiments, Progr. NMR Spectrosc. 16 (1983) 163192.
[8] R.R. Ernst, G. Bodenhausen, A. Wokaun, Principles of nuclear magnetic resonance in one and two dimensions, Clarendon Press, Oxford, 1987.
[9] I.S. Podkorytov, Multipulse NMR Part II. product operator description of the weakly coupled, two-spin-1/2 system, Concepts Magn. Reson. 9 (3) (1997) 117-137.
[10] N. Chandrakumar, in: E. Fluck, H. Günter (Eds.), Basic Principles and Progress in NMR, vol. 34, Springer-Verlag, Berlin, 1996.
[11] A. Gençten, Ö. Tezel, S. Bahçeli, Product operator theory for spin-3/2 nuclei and application to 2D-J resolved NMR spectroscopy, Chem. Phys. Lett. 351 (2002) 109-114.
[12] Ö. Tezel, A. Gençten, A. Tokatli, M. Şahin, S. Bahçeli, A theoretical investigation of distortionless enhancement by polarization transfer and subspectral editing with a multiple quantum trap NMR Spectroscopy for $\mathrm{CX}_{\mathrm{N}}$ groups, Acta Phy. Pol. A 104 (2003) 503-511.
[13] O.W. Sorensen, R.R. Ernst, Elimination of spectral distortion in polarization transfer experiments. Improvements and comparison of techniques, J. Magn. Reson. 51 (1983) 477-489.
[14] N. Chandrakumar, Polarization transfer between spin-1 and spin1/2 nuclei, J. Magn. Reson. 60 (1984) 28-36.
[15] S.K. Lee, B.K. Nicholson, Bis- and Tris-(pyrazolyl)borate complexes of methyltinchlorides and the X-ray structure of fivecoordinate [bis(pyrazolyl)borate]chlorodimethyltin(IV), J. Organomet. Chem. 309 (1986) 257-265.
[16] J. Lorberth, S. Wocadlo, W. Massa, E.V. Grigoriev, S. Yashina, V.S. Petrosyan, P. Finocchiaro, Synthesis and structure of $1: 1$ complexe of dimethyltindichloride with meso-1,2-bis( $\alpha$-diethoxyphosphorylbenzylamino)ethane, J. Organomet. Chem. 510 (1996) 287-290.
[17] J.W. Akitt, W.S. Mc Donald, Arrangements of ligands giving low electric field gradients, J. Magn. Reson. 58 (1984) 401412.
[18] J.C.P. Sanders, G.J. Schrobilgin, in: P. Granger, R.K. Harris (Eds.), Multinuclear Magnetic Resonance in Liquids and Solidschemical Applications, Kluwer Academic, Dordrecht, 1990, p. 157.
[19] C. Brevard, P. Granger, Handbook of High Resolution Multinuclear NMR, Wiley, New York, 1981.
[20] A. Heck, Introduction to Maple, Second ed., Springer-Verlag, New York, 1997.
[21] S.W. Homans, A Dictionary of Concepts in NMR, Clarendon Press, Oxford, 1992.
[22] P.L. Rinaldi, N.J. Baldwin, Selective excitation and sensitivity enhancement of ${ }^{1} \mathrm{H}$ resonances by polarization transfer from low gamma quadrupolar nuclei, J. Magn. Reson. 61 (1985) 165-167.


[^0]:    * Corresponding author.

    E-mail address: bahceli@fef.sdu.edu.tr (S. Bahçeli).
    ${ }^{1}$ Present address: Department of Physics, Faculty of Education, Osmangazi University, Eskisehir, Turkey.

